

# Study of the $e^+e^- \rightarrow \eta\gamma$ process with SND detector at the VEPP-2M $e^+e^-$ collider

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In experiment with the SND detector at the VEPP-2M  $e^+e^-$  collider the  $e^+e^- \rightarrow \eta\gamma$  cross section was measured in the center-of-mass energy range  $E=0.60\text{--}1.38$  GeV with the integrated luminosity of  $27.8\text{ pb}^{-1}$ . The measured cross section is well described by the vector meson dominance model with contributions from the  $\rho(770)$ ,  $\omega(783)$ ,  $\phi(1020)$ ,  $\rho'(1465)$  resonances and agrees with results of previous measurements. The decay probabilities  $\mathcal{B}(\phi \rightarrow \eta\gamma)$ ,  $\mathcal{B}(\omega \rightarrow \eta\gamma)$  and  $\mathcal{B}(\rho \rightarrow \eta\gamma)$  were measured with the accuracies better than or comparable to the world averages.

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## I. INTRODUCTION

Measurements of the vector mesons radiative decays  $\rho$ ,  $\omega$ ,  $\phi \rightarrow \pi^0\gamma$ ,  $\eta\gamma$  were subject of experimental investigation in several tens of experiments during more than 40 years [1]. However, further improvement of accuracy of these branching ratios measurements is still important for development of various phenomenological models — quark models, SU(3) based linear and non-linear sigma models and vector meson dominance models, [2, 3, 4].

The vector meson radiative decays give information on the underlying non-perturbative QCD dynamics and this is one reason why interest in such decays is still not exhausted. The  $\eta$  meson is a member of the low-lying pseudoscalar octet and therefore is a would-be Goldstone boson associated with the spontaneous breaking of chiral symmetry in the QCD vacuum. Besides it is significantly connected to the  $\eta'$  meson which by itself is strongly affected by QCD axial anomaly. Therefore any information about the  $\eta$  meson structure, and the vector mesons radiative decays are one of sources of such information, will give a clue about the QCD vacuum and mechanisms of the chiral symmetry breaking.

Theoretically radiative decays with the  $\eta\gamma$  final state were investigated in the context of a quark-level linear sigma model [5], using QCD sum rules [6] and in the framework of the non-relativistic quark model [7].

Another interesting theoretical problem where the high precision experimental input from the vector meson radiative decays is welcome is the  $\eta - \eta'$  mixing problem. As the experimental data became more precise it turned out that the traditional one mixing angle scheme does not work properly and more sophisticated two mixing angle description was developed [8]. The physics underlying  $\eta$  and  $\eta'$  mesons constitutes a vivid and fascinating research field today providing unexpected challenges and surprises [9].

The best accuracy in measurement of the decay probabilities  $\rho$ ,  $\omega$ ,  $\phi \rightarrow \eta\gamma$  was achieved in the last  $e^+e^-$  storage ring experiments with CMD-2 [10, 11, 12] and SND [13, 14, 15, 16, 17] detectors through investigation of the  $e^+e^- \rightarrow \rho$ ,  $\omega$ ,  $\phi \rightarrow \eta\gamma$  processes. The reached accuracy is of the order of 10% for the decays  $\rho$ ,  $\omega \rightarrow \eta\gamma$  and about 2% for the  $\phi \rightarrow \eta\gamma$  decay, and the last result has been obtained by averaging more than 10 measurements with accuracies of the order of 5% each.

In this paper we present results of our studies of the process

$$e^+e^- \rightarrow \eta\gamma, \quad (1)$$

with the subsequent decays of the  $\eta$  meson into the three-pion final states:

$$\eta \rightarrow 3\pi^0 \quad (2)$$

$$\eta \rightarrow \pi^+\pi^-\pi^0. \quad (3)$$

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Experimental data with integrated luminosity of  $27.8 \text{ pb}^{-1}$  collected in experiments with the SND detector at the VEPP-2M collider in the center-of-mass energy range  $E=0.60\text{--}1.38 \text{ GeV}$  were analyzed.

The aim of the present work is to increase the accuracy of measurements of the decay probabilities  $\rho$ ,  $\omega$ ,  $\phi \rightarrow \eta\gamma$ , and also to measure the cross section in the non-resonant region, in particular, at energies above the  $\phi$ -meson resonance.

## II. THE SND DETECTOR

The general purpose non-magnetic detector SND [18] was developed for experiments at VEPP-2M  $e^+e^-$  collider. The basic part of SND is a three layer electromagnetic calorimeter consisting of 1632 NaI(Tl) crystals. Total thickness of the calorimeter is 13.4 radiation lengths. The calorimeter covers nearly 90% of the full solid angle:  $18^\circ \leq \theta \leq 162^\circ$ , where  $\theta$  is the polar angle. Dependence of the energy resolution of the calorimeter on energy of the photon is given by the formula  $\sigma_E/E_\gamma(\%) = 4.2\%/\sqrt[4]{E_\gamma(\text{GeV})}$ , while the angular resolution is  $\sigma_\varphi = 0.82/\sqrt{E_\gamma(\text{GeV})} \oplus 0.63$  degrees.

For determination of charged particles production angles, two coaxial cylindrical drift chambers are used. The angular resolution is  $1.8^\circ$  in polar direction, and  $0.53^\circ$  in the azimuthal direction.

Experiments were performed in 1995–2000 in the energy range  $E=0.38\text{--}1.38 \text{ GeV}$ . The statistics was collected by repeated scanning of the energy range with variable step. Integrated luminosity was measured using elastic scattering and two-photon annihilation with 2% accuracy. In total the SND detector recorded about  $1.5 \times 10^9$  events. From them about  $10^7$  are events with  $\phi$ -meson production and decay,  $3.7 \times 10^6$  with the  $\omega$ -meson production, and  $7 \times 10^6$  with the  $\rho$ -meson production.

## III. SELECTION OF EVENTS IN THE DECAY CHANNEL $\eta \rightarrow 3\pi^0$

Selection of events of the process under study (1) in the decay mode (2) was performed in several steps. At the first stage the events satisfying the following conditions were selected:

1.  $N_\gamma \geq 6$ , where  $N_\gamma$  is the number of reconstructed photons in an event;
2.  $N_c = 0$ , where  $N_c$  is the number of reconstructed charged particle tracks;
3.  $0.7 < E_{tot}/E < 1.2$ , where  $E_{tot}$  is the total energy deposition in the calorimeter;
4.  $cP_{tot}/E < 0.2$ , where  $P_{tot}$  is the total momentum of photons;
5.  $(E_{tot} - cP_{tot})/E > 0.7$ .

We allow a loss of one soft photon from 7 final photons of the  $e^+e^- \rightarrow \eta\gamma \rightarrow 3\pi^0\gamma$  reaction. Besides, we accept events with extra photons ( $N_\gamma > 7$ ). The extra photons appear as a result of shower splitting in the calorimeter or superimposed machine background. Since the final state of the process under study includes only photons, the energy deposition in the calorimeter and the total photon momentum (magnitude of the vector sum of photon momenta) are close to  $e^+e^-$  center-of-mass energy and zero, respectively. Fig.1 shows two-dimensional distribution of these parameters for data events, and Monte-Carlo (MC) simulated events of signal and background processes. The line indicates the selection cuts 3, 4 and 5. With the use of these criteria, 47676 events have been selected.

As the background sources one has the following processes

$$e^+e^- \rightarrow K_S K_L, \quad K_S \rightarrow 2\pi^0, \quad (4)$$

$$e^+e^- \rightarrow \pi^0\pi^0\gamma, \quad (5)$$

$$e^+e^- \rightarrow \omega\pi^0\pi^0, \quad \omega \rightarrow \pi^0\gamma. \quad (6)$$

Analysis of the experimental data has shown that the quantum-electrodynamic events from processes with large cross sections, for example:

$$e^+e^- \rightarrow 2(3)\gamma, \quad (7)$$

also can give the required event configuration when the machine background is superimposed on them. The contributions of other background processes are negligible.

For events selected at the first stage, kinematic fits using the measured photon angles and energies, and energy-momentum conservation laws, were performed. The quality of each kinematic fit is characterized by the parameter  $\chi^2$ . Five kinematic hypotheses were checked:

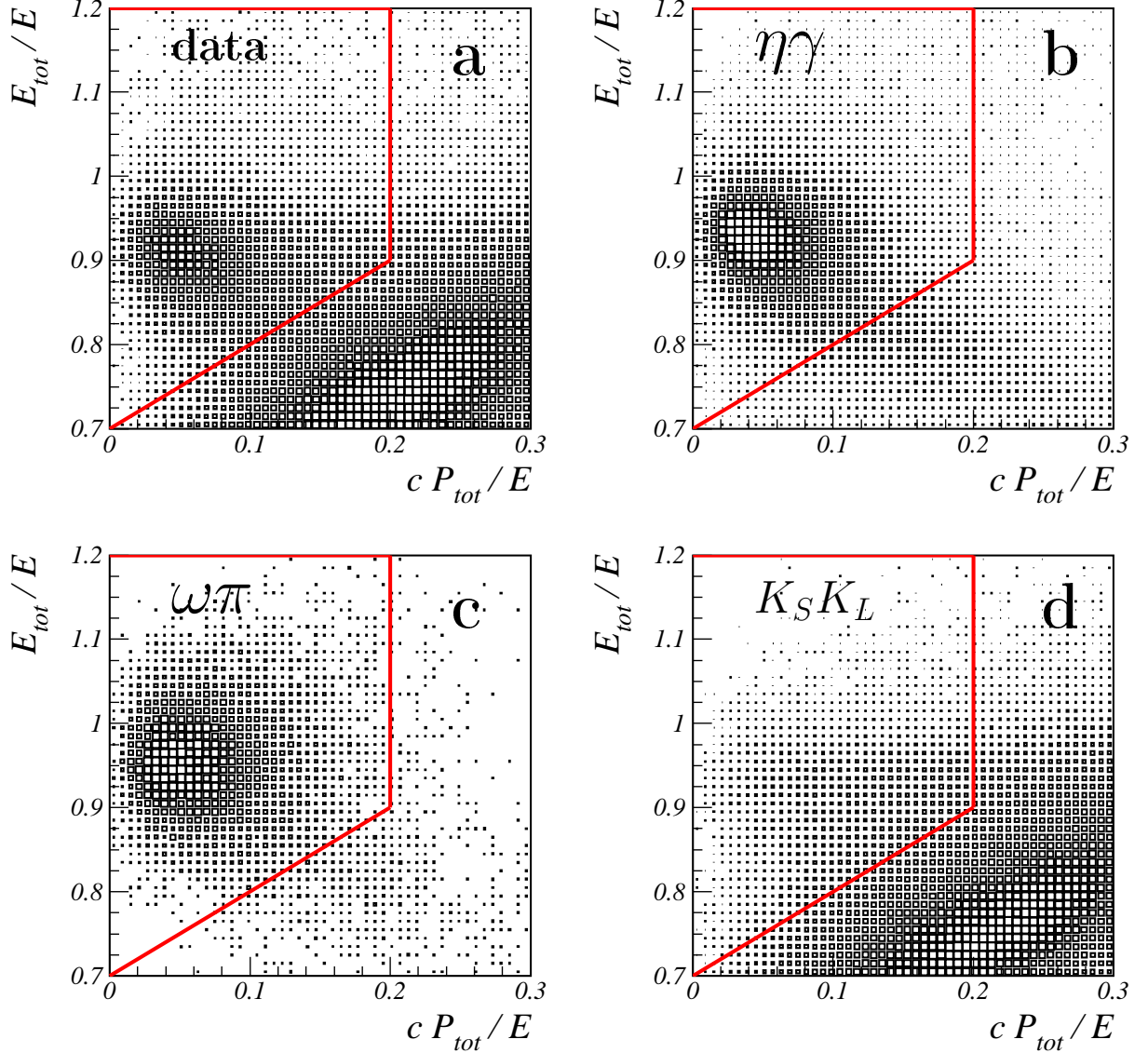


FIG. 1: Two-dimensional distributions of normalized calorimeter energy deposition vs. normalized total momentum of the detected particles for the selected data events in the whole energy region (a) and for simulated events of the signal and background processes (b,c,d). Solid lines indicate the selection cuts.

1.  $e^+e^- \rightarrow n\gamma$ ,  $n \geq 6$  ( $\chi_{n\gamma}^2$  – the corresponding parameter),
2.  $e^+e^- \rightarrow \eta\gamma \rightarrow 3\pi^0\gamma \rightarrow 7\gamma$  ( $\chi_{\eta\gamma}^2$ ),
3.  $e^+e^- \rightarrow 3\gamma$  ( $\chi_{3\gamma}^2$ ),
4.  $e^+e^- \rightarrow \pi^0\pi^0\gamma$  ( $\chi_{\pi^0\pi^0\gamma}^2$ ),
5.  $e^+e^- \rightarrow \omega\pi^0\pi^0 \rightarrow 3\pi^0\gamma \rightarrow 7\gamma$  ( $\chi_{\omega\pi^0\pi^0}^2$ ).

In hypotheses 2, 4, 5 additional constraints on invariant masses of the photon pairs and on the invariant mass of the  $\pi^0\gamma$  system were applied. In case when the number of detected photons in the event exceeded the number of photons necessary for the given hypothesis, kinematic fit was performed for all possible photon combinations and the one with the lowest  $\chi^2$  value was selected.

In the energy region below 1 GeV the process  $e^+e^- \rightarrow \eta\gamma$ ,  $\eta \rightarrow 3\pi^0$  is the only process with a significant cross section and multi-photon final state. In the  $\phi$ -meson region there is a contribution from the process (4). Since this energy region is above the  $\omega\pi^0$  production threshold, there is also a background from the process (5).

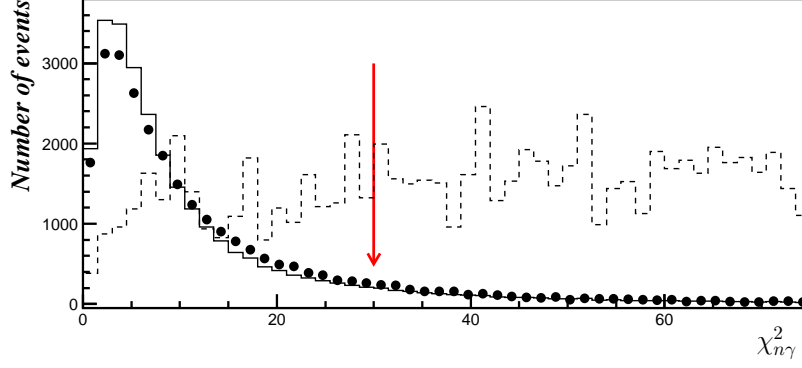


FIG. 2: The  $\chi^2_{n\gamma}$  distributions for data events with  $E < 1.06$  GeV (points with error bars). The dashed histogram shows the expected distribution for background processes (4) and (5) scaled by a factor of 100. The solid histogram shows the sum of simulated signal and background distributions. The data and simulated distributions are normalized to the same area. The cut on  $\chi^2_{n\gamma}$  is indicated by the arrow.

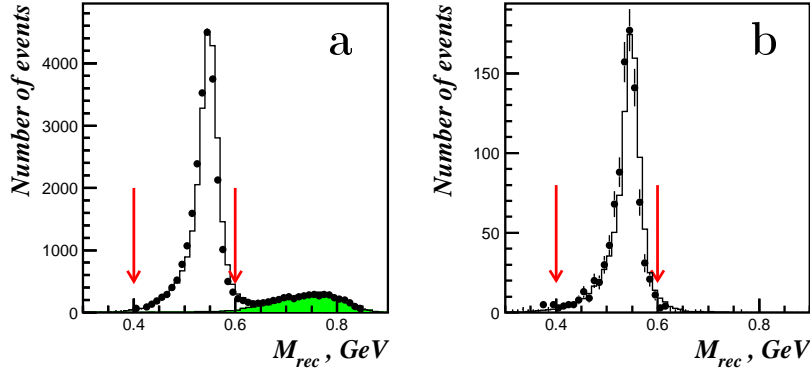


FIG. 3: Recoil mass of the most energetic photon in  $e^+e^- \rightarrow n\gamma$  ( $n \geq 6$ ) events. a)  $\phi$ -meson region; b)  $\omega$  and  $\rho$  mesons region. The histogram shows MC simulation of the process  $e^+e^- \rightarrow \eta\gamma$ ,  $\eta \rightarrow 3\pi^0$ . The shaded histogram shows simulation of all background processes. Points with error bars are data. Vertical arrows indicate the cut on  $M_{rec}$  used for final selection of signal events.

For separation of events of the process (1) at  $E < 1.06$  GeV and suppression of the background from processes (4), (5) and (7), the following cuts on the  $\chi^2$  parameters were imposed:

1.  $\chi^2_{n\gamma} < 30$  ;
2.  $\chi^2_{3\gamma} > 20$  ;
3.  $\chi^2_{\pi^0\pi^0\gamma} > 20$  .

The distributions of  $\chi^2_{n\gamma}$  for data events and simulated signal and background events are shown in Fig. 2.

After applying these selections criteria about  $32 \times 10^3$  events were left for further analysis. The recoil mass distribution of the most energetic photon  $M_{rec}$  is presented in Fig. 3 for energies close to the  $\omega$  and  $\phi$  resonances. Events in Fig.3b with  $M_{rec} > 0.6$  GeV are attributed to the process (4). Final selection of events was carried out with the cut  $0.4 < M_{rec} < 0.6$  GeV.

The contribution of the background process (4) for each energy point in the  $\phi$ -meson region was determined as follows:

$$N_{K_S K_L} = N_{K_S K_L}^{data}(0.6 < M_{rec} < 0.8) \frac{N_{K_S K_L}^{MC}(0.4 < M_{rec} < 0.6)}{N_{K_S K_L}^{MC}(0.6 < M_{rec} < 0.8)}, \quad (8)$$

where  $N_{K_S K_L}^{MC}(0.4 < M_{rec} < 0.6)$  and  $N_{K_S K_L}^{MC}(0.6 < M_{rec} < 0.8)$  are number of MC simulated events of the process (4) with recoil mass of the most energetic photon in intervals 0.4–0.6 GeV and 0.6–0.8 GeV, respectively.  $N_{K_S K_L}^{data}(0.6 <$

$M_{rec} < 0.8$ ) is the number of data events with  $0.6 < M_{rec} < 0.8$  GeV. The contribution of the background process (4) for the energy points in the range 1.00 – 1.03 GeV is about 1.2% of the total number of selected events at each point. The systematic error on the background event number from the process (4) is 40%. It was estimated as a difference between the calculation with the formula (8) and direct estimation by simulation.

In the energy range from 1.06 GeV (the  $\omega\pi^0\pi^0$  production threshold) up to 1.40 GeV the contribution of the background process (6) is comparable to that of signal process (1). The kinematics of events (6) closely resembles the kinematics of events (1), which complicates the suppression of the background related to the process (6). Therefore, additional selection criteria were applied to events in the energy region  $E > 1.06$  GeV:

1.  $N_\gamma = 7$ ,
2.  $\chi_{\eta\gamma}^2 < 60$ ,
3.  $\chi_{\eta\gamma}^2 - \chi_{\omega\pi^0\pi^0}^2 < 0$ .

With these conditions 47 events with energy  $E > 1.06$  GeV were selected (Tables III, IV).

The estimation based on measured cross section of the process (6) [19] and its detection efficiency determined from the MC simulation for selection criteria described above shows that the background from the process (6) is negligible.

#### IV. SELECTION OF EVENTS IN THE $\eta \rightarrow \pi^+\pi^-\pi^0$ DECAY MODE

For selection of events of the signal process (1) in the decay mode (3), the following selection criteria were applied at the first stage:

1.  $N_c = 2$ ,
2.  $N_\gamma \geq 3$ ,
3.  $R_i < 0.25\text{cm}$ , where  $R_i$  is the distance between the  $i$ -th charged particle track and the beam axis,
4.  $|Z_i| < 10\text{cm}$ , where  $Z_i$  is the coordinate of the charged particle production point along the beam axis.

The main background process at energies near and below the  $\phi$  resonance is the process

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0 \quad (9)$$

with an extra photon from beam background, photon radiation by initial or final particles or nuclear interaction of the charged pions with the detector material. In the energy region above the  $\phi$  meson, the main background contribution is expected from the process

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0. \quad (10)$$

For energies above 1.06 GeV this background significantly exceeds the signal, thus the process (1) in the mode (3) was not studied at energies above 1.06 GeV.

For about  $3.7 \times 10^5$  events selected with the above-stated criteria in the energy range  $E \leq 1.06\text{GeV}$ , the kinematic fit was performed in two hypotheses:

1.  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma \rightarrow \pi^+\pi^-\gamma\gamma\gamma$  ( $\chi_{3\pi\gamma}^2$ ),
2.  $e^+e^- \rightarrow \pi^+\pi^-\pi^0 \rightarrow \pi^+\pi^-\gamma\gamma$  ( $\chi_{3\pi}^2$ ).

For selection of events of the process  $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma$  and suppression of the background from the process (9) the following cuts were used:

1.  $\chi_{3\pi\gamma}^2 < 25$ ,
2.  $\chi_{3\pi}^2 > 50$ .

Distributions of the selected events over the recoil mass of the photon, which is not included into the reconstructed  $\pi^0$ -meson, are shown in Fig. 4 for three energy points. Events of the process (1) form a narrow peak near the  $\eta$ -meson mass. Events of the background process (9) have the distribution which is well described by a linear function in the recoil mass interval 0.45–0.7 GeV.

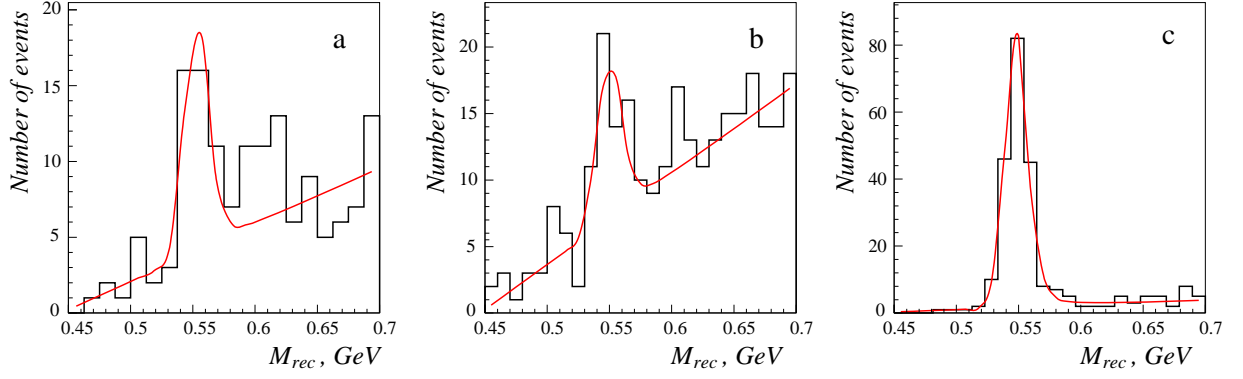


FIG. 4: Distributions of the recoil mass of the photon not included into the reconstructed  $\pi^0$ -meson for selected data events (histogram). The curve represents the result of the fit described in the text. a)  $E = 0.764\text{--}0.774$  GeV; b)  $E = 0.784$  GeV; c)  $E = 1.022$  GeV.

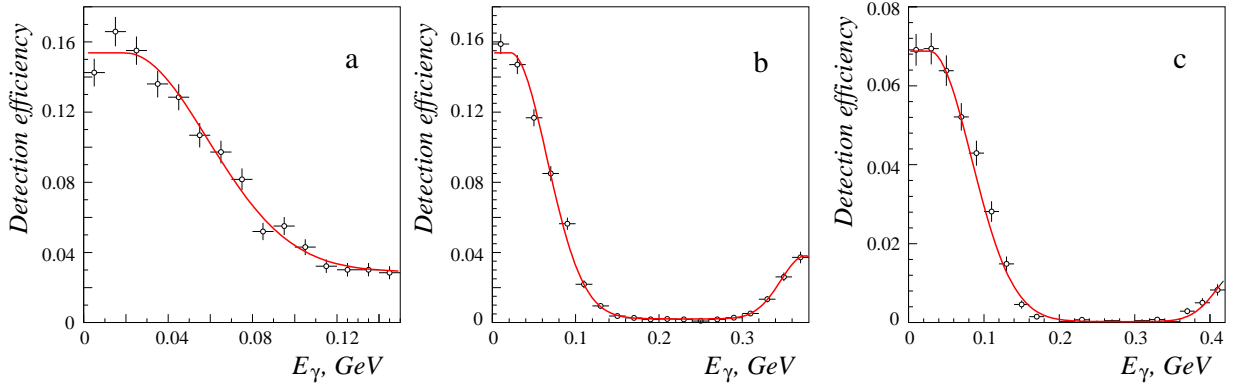


FIG. 5: The dependence of the detection efficiency of the process  $e^+e^- \rightarrow \eta\gamma, \eta \rightarrow 3\pi^0$  on the energy of the initial state radiation photon. a)  $E < 0.88$  GeV; b)  $0.88 \leq E \leq 1.06$  GeV; c)  $E > 1.06$  GeV.

The number of events of the process  $e^+e^- \rightarrow \eta\gamma \rightarrow \pi^+\pi^-\pi^0\gamma$  in each energy point was determined by approximating the recoil mass spectra by a sum of the signal and background distributions. For the description of the shape of the signal spectrum so called Novosibirsk function [20] was used which parameters (the width and asymmetry) were taken from simulation. Comparison of the  $\eta$  line-shapes for the simulated and data events was performed in the energy range close to the  $\phi$ -meson resonance (Fig. 4c) and it was shown that the simulation reproduces the data shape with sufficient accuracy. The recoil photon spectrum for the background events was approximated either by a linear function or by a parabola. The difference between the results of approximations with two different shapes of the background was used for the estimation of the associated systematic error. The obtained numbers of events for different energy points are listed in the Table V. The quoted errors are statistical and systematic, respectively. For a part of the data points the statistics of neighboring energy points were summed together. In this case the boundaries of the energy interval are shown in the Table V.

## V. DETECTION EFFICIENCY

Detection efficiency for the process under study was determined from Monte-Carlo simulation which takes into account the radiative corrections due to photon radiation by initial particles [21]. Angular distribution of these photons was modeled according to the work [22]. The detection efficiency was evaluated as a function of two parameters: the center-of-mass energy and the energy of the additional photon  $E_\gamma$ . Fig.5 shows the dependence of the detection efficiency of the process  $e^+e^- \rightarrow \eta\gamma, \eta \rightarrow 3\pi^0$  on  $E_\gamma$ . When the “lost energy”  $E_\gamma$  increases, the efficiency falls at first and then increases again. Such behavior is due to the presence of two different photons in an event: one from the vector meson decay  $V \rightarrow \eta\gamma$  and the another from the initial state radiation. As the initial state radiation photon reaches its highest allowed energy, it starts to substitute the decay photon, which becomes soft. In fact the number of events from this kinematic region is negligible due to low probability of hard photon emission and very low  $e^+e^- \rightarrow \eta\gamma$

cross section at threshold.

Detection efficiency values  $\epsilon(E, E_r)$  were calculated in each energy point for both decay channels of the  $\eta$ -meson (2) and (3). The efficiency obtained from the simulation was corrected to take into account the difference of the detector response simulation from reality. The evaluation of correction factors is described in the section VII.

The visible cross section of the process  $e^+e^- \rightarrow \eta\gamma$  can be written as

$$\sigma_{vis}(E) = \int_0^{x_{max}} \epsilon_r(E, \frac{xE}{2}) F(x, E) \sigma(\sqrt{1-x}E) dx, \quad (11)$$

where  $\sigma(E)$  is the Born cross section, which one needs to extract from the experiment,  $F(x, E)$  is a function describing a probability distribution of the energy fraction  $x = 2E_r/E$  [21] taken away by the additional photon. Equation (11) can be rewritten in the traditional form:

$$\sigma_{vis}(E) = \epsilon(E) \sigma(E) (1 + \delta(E)), \quad (12)$$

where the parameter  $\epsilon(E)$  is defined as follows:

$$\epsilon(E) \equiv \epsilon_r(E, 0), \quad (13)$$

and  $\delta(E)$  is the radiative correction.

Technically the determination of the Born cross sections is performed as follows. With the use of formula (11) the energy dependence of the measured visible cross section is approximated. For that the Born cross section is parametrized by some theoretical model describing the data well. With the use of the obtained parameters of the model, the radiative correction is determined and then with the formula (12) the experimental Born cross section  $\sigma$  is calculated. To estimate the model dependence of the radiative correction due to the choice of cross section approximation function, several models of the Born cross section parametrization are used.

## VI. CROSS SECTION PARAMETERIZATION

Energy dependence of the  $e^+e^- \rightarrow \eta\gamma$  Born cross section was parameterized according to the vector meson dominance model:

$$\sigma_{\eta\gamma}(E) = \frac{q(E)^3}{E^3} \left| \sum_{V=\rho, \omega, \phi, \rho'} A_V(E) \right|^2, \quad A_V(E) = \frac{m_V \Gamma_V e^{i\varphi_V}}{D_V(E)} \sqrt{\frac{m_V^3}{q(m_V)^3} \sigma_{V\eta\gamma}}, \quad (14)$$

$$D_V(E) = m_V^2 - E^2 - iE\Gamma_V(E), \quad q(E) = \frac{E}{2} \left( 1 - \frac{m_\eta^2}{E^2} \right).$$

Here  $m_V$  is the resonance mass,  $\Gamma_V(E)$  is its full width which depends on energy ( $\Gamma_V \equiv \Gamma_V(m_V)$ ),  $\sigma_V = 12\pi\mathcal{B}(V \rightarrow e^+e^-)/m_V^2$  and  $\sigma_{V\eta\gamma} = \sigma_V\mathcal{B}(V \rightarrow \eta\gamma)$  are Born cross sections of the  $e^+e^- \rightarrow V$  and  $e^+e^- \rightarrow V \rightarrow \eta\gamma$  processes at  $E = m_V$ ,  $\mathcal{B}(V \rightarrow e^+e^-)$  and  $\mathcal{B}(V \rightarrow \eta\gamma)$  are branching fractions of the corresponding decays,  $\varphi_V$  are interference phases ( $\varphi_\rho \equiv 0$ ).

At approximations of the data, the free parameters were  $\sigma_{\rho\eta\gamma}$ ,  $\sigma_{\omega\eta\gamma}$ ,  $\sigma_{\phi\eta\gamma}$  and the phases  $\varphi_\omega$ ,  $\varphi_\phi$ . In the energy region above the  $\phi$ -meson resonance it is necessary to take into account contributions from decays of the radial excitations of the  $\rho$ ,  $\omega$  and  $\phi$  mesons. As the experimental statistics in this energy region is scarce, we restricted ourselves to introduction of just one additional resonance with the mass  $M_{\rho'} = 1.465$  GeV and width  $\Gamma_{\rho'} = 0.4$  GeV. The cross section at the resonance  $\sigma_{\rho'\eta\gamma}$  and the phase  $\varphi_{\rho'}$  were also free parameters.

## VII. SYSTEMATIC UNCERTAINTIES

The systematic errors on the measured Born cross section include the contributions of uncertainties in the detection efficiency, the luminosity measurement, and systematic errors of the background subtraction which were discussed above.

To take into account imperfect modeling of the detector response, the detection efficiency determined from simulation was multiplied by a correction factor. It was evaluated using events from the energy interval in the vicinity of the  $\phi$ -meson resonance where the process (1) can be extracted with low background by application of the selection criteria less stringent than those described in Section III. In particular, we can exclude the condition  $\chi_{n\gamma}^2 < 30$  and calculate the corresponding correction factor (connected with the application of this condition) as follows:

$$r_{\chi_{n\gamma}^2} = \frac{N_{data}(\chi_{n\gamma}^2 < 30)}{N_{MC}(\chi_{n\gamma}^2 < 30)} \frac{N_{MC}}{N_{data}},$$

where  $N_{data}$ ,  $N_{MC}$  are event numbers in the data and simulation, respectively, without the cut on  $\chi_{n\gamma}^2$ ,  $N_{data}(\chi_{n\gamma}^2 < 30)$ ,  $N_{MC}(\chi_{n\gamma}^2 < 30)$  are numbers of events with  $\chi_{n\gamma}^2 < 30$ . For data events the preliminary subtraction of the background from the process  $e^+e^- \rightarrow K_S K_L$  was performed. Analogous corrections were calculated for all other selection conditions used in the analysis. The overall correction factors for the mode (2) were  $0.990 \pm 0.004$  and  $0.952 \pm 0.004$  for selection criteria used for energies  $E < 1.06$  GeV and  $E > 1.06$  GeV, respectively. Since the fraction of events rejected by the selection cuts is practically independent on energy, the correction found at  $\phi$ -meson was applied to all energies. The uncertainty of the correction factor was included into the detection efficiency uncertainty.

As it was discussed earlier, additional “false” photons appear in the SND calorimeter because of beam-background pile-up. To take into account this effect in the Monte-Carlo simulation, actual events recorded with special random trigger were merged with simulated events in proper proportion. Unaccounted difference in photon multiplicities between data and simulation can lead to an additional uncertainty in the detection efficiency. Another effect which is not compensated by the correction factor considered above is a possible inaccuracy of the calorimeter response modeling near the calorimeter edges.

To estimate the influence of these effects we analyzed events with additional conditions  $N_\gamma \geq 7$  and  $\theta_\gamma \geq 36^\circ$ , where  $\theta_\gamma$  is a polar angle of the detected photon. The following ratios have been calculated:

$$r_{N_\gamma} = \frac{N_{data}(N_\gamma \geq 7)}{N_{MC}(N_\gamma \geq 7)} \frac{N_{MC}}{N_{data}} = 0.989 \pm 0.008,$$

$$r_{\theta_\gamma} = \frac{N_{data}(\theta_\gamma > 36^\circ)}{N_{MC}(\theta_\gamma > 36^\circ)} \frac{N_{MC}}{N_{data}} = 1.016 \pm 0.010.$$

Although both ratios are compatible with unity, we use their deviations from unity as estimates of the systematic uncertainties connected with discrepancies of the photon multiplicity and edge effects modeling.

Thus the total systematic error of the detection efficiency for the mode (2) is estimated to be 1.9%.

For the decay mode (3), the total correction factor for the detection efficiency turned out to be  $0.942 \pm 0.08$ . The uncertainty due to the “edge effect” was taken from the analysis of the channel (2). The total systematic error for the decay mode (3) is 1.8%.

The integrated luminosity was determined by using two QED processes  $e^+e^- \rightarrow e^+e^-$  and  $e^+e^- \rightarrow \gamma\gamma$  which cross sections are known with accuracy better than 1%. The difference between these two luminosity measurements was used as an estimate of the systematic uncertainty of the luminosity determination. It is 2% and practically independent of the beam energy.

The uncertainty in the the radiative correction calculation includes the theoretical uncertainty which does not exceed 0.1% [21], and the model uncertainty, which is also 0.1%.

## VIII. RESULTS OF THE CROSS SECTION APPROXIMATION

Before carrying out approximation of the cross section energy dependence, the ratio of the  $\eta$ -meson decay probabilities in two  $\eta$  decay modes was calculated from the corresponding event numbers and detection efficiencies. It was found that the ratio does not depend on the beam energy. Therefore combined approximation of the visible cross sections measured in two decay modes was performed. For the decay probabilities  $\eta \rightarrow 3\pi^0$  and  $\pi^0 \rightarrow 2\gamma$  the world-average values [1] were used, the ratio of the decay probabilities  $\eta \rightarrow 3\pi^0$  and  $\eta \rightarrow \pi^+\pi^-\pi^0$  was a free parameter. As a result of the approximation the following value of this ratio has been obtained

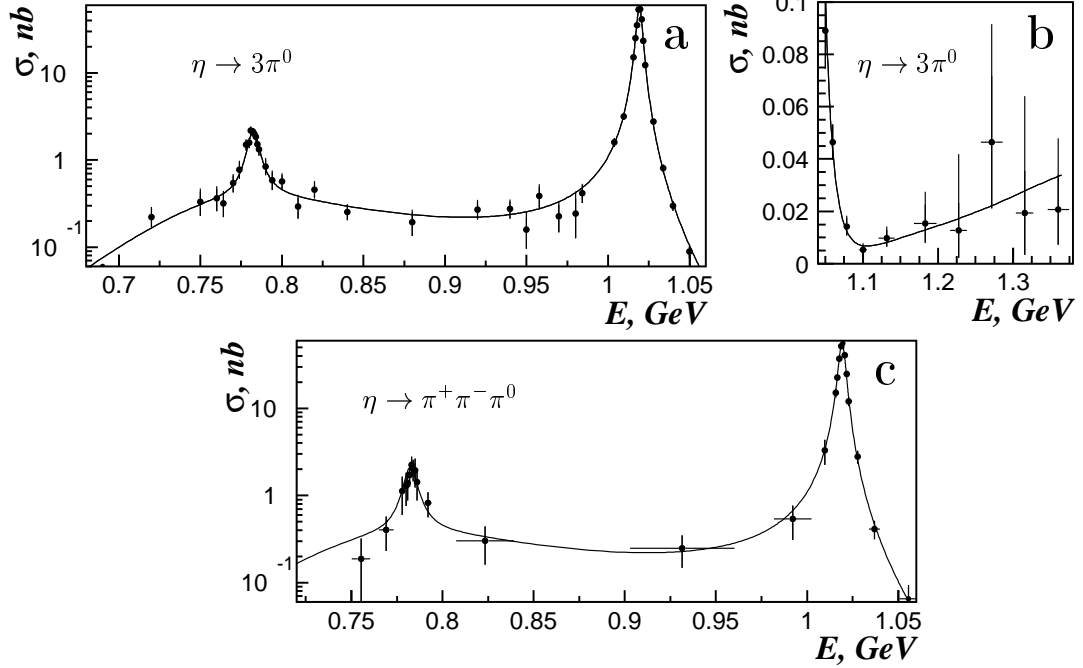
$$\frac{\mathcal{B}(\eta \rightarrow 3\pi^0)}{\mathcal{B}(\eta \rightarrow \pi^+\pi^-\pi^0)} = 1.46 \pm 0.03 \pm 0.09,$$

The systematic error includes uncertainties in the detection efficiency, the luminosity measurement, and the systematic error in the number of selected events. Our result is in a good agreement with the world-average value [1],  $1.44 \pm 0.04$ .



TABLE I: Results of approximation. The first error is statistical, the second systematic.

$\sigma_{\rho\eta\gamma}$	$(0.273 \pm 0.029 \pm 0.006) \text{ nb}$
$\sigma_{\omega\eta\gamma}$	$(0.797 \pm 0.079 \pm 0.017) \text{ nb}$
$\varphi_{\omega}$	$(11.3 \pm 8.1 \pm 0.3)^{\circ}$
$\sigma_{\phi \rightarrow \eta\gamma}$	$(57.14 \pm 0.79 \pm 1.26) \text{ nb}$
$\varphi_{\phi}$	$(170 \pm 12 \pm 4)^{\circ}$
$\sigma_{\rho'\eta\gamma}$	$(0.020^{+0.019}_{-0.013} \pm 0.001) \text{ nb}$
$\varphi_{\rho'}$	$(61^{+39}_{-20} \pm 2)^{\circ}$
$\chi^2_{3\pi^0}/ndf$	31/41
$\chi^2_{\pi^+\pi^-\pi^0}/ndf$	9.8/19

FIG. 6: Cross section of the process  $e^+e^- \rightarrow \eta\gamma$  measured in the  $\eta \rightarrow 3\pi^0$  decay mode (a,b) and the  $\eta \rightarrow \pi^+\pi^-\pi^0$  decay mode (c).

Further approximation was performed with this ratio fixed at the world-average value but with its uncertainty taken into account.

Values of the cross sections at the resonance maximums and the interference phases obtained as a result of approximation are presented in the Table I.

The cross section of the  $e^+e^- \rightarrow \eta\gamma$  process in the modes  $\eta \rightarrow 3\pi^0$  and  $\eta \rightarrow \pi^+\pi^-\pi^0$  is shown in Fig.6 and in the Tables III, IV, and V. Using the world-average values [1] for the masses and for the decay probabilities  $\rho, \omega, \phi \rightarrow e^+e^-$  we can calculate the decay probabilities into the  $\eta\gamma$  final state:

$$\begin{aligned}
 \mathcal{B}(\rho \rightarrow \eta\gamma) &= (2.40 \pm 0.25 \pm 0.07) \times 10^{-4}, \\
 \mathcal{B}(\omega \rightarrow \eta\gamma) &= (4.63 \pm 0.46 \pm 0.13) \times 10^{-4}, \\
 \mathcal{B}(\phi \rightarrow \eta\gamma) &= (1.362 \pm 0.019 \pm 0.035) \times 10^{-2}.
 \end{aligned}$$

TABLE II: The values of  $\rho, \omega, \phi \rightarrow \eta\gamma$  branching fractions obtained in this work (second column) and in the most precise previous experiments (third column). The first error is statistical, the second systematic. The current world-average value are listed in the fourth column.

	This work	Previous measurements	PDG [1]
$\mathcal{B}(\rho \rightarrow \eta\gamma) \times 10^4$	$2.40 \pm 0.25 \pm 0.07$	$3.28 \pm 0.37 \pm 0.23$ [11]	$3.0 \pm 0.4$
$\mathcal{B}(\omega \rightarrow \eta\gamma) \times 10^4$	$4.63 \pm 0.46 \pm 0.13$	$5.10 \pm 0.72 \pm 0.34$ [11]	$4.9 \pm 0.5$
$\mathcal{B}(\phi \rightarrow \eta\gamma) \times 10^2$	$1.362 \pm 0.019 \pm 0.035$	$1.338 \pm 0.012 \pm 0.52$ [15]	$1.295 \pm 0.025$

## IX. CONCLUSION

In the present work the cross section of the process  $e^+e^- \rightarrow \eta\gamma$  was measured in the decay modes  $\eta \rightarrow 3\pi^0$  and  $\eta \rightarrow \pi^+\pi^-\pi^0$  in the energy range 0.60–1.38 GeV. The obtained data agree with the results of previous measurements [10, 11, 12, 13, 14, 15, 16, 17].

The measured cross section is well described by the vector meson dominance model with contributions from  $\rho(770)$ ,  $\omega(783)$ ,  $\phi(1020)$ , and their excitations, represented in our fit to data by  $\rho'(1465)$ . As a result of the data approximation we obtained the  $\rho, \omega, \phi \rightarrow \eta\gamma$  decay probabilities listed in Table II together with the world-average values and most precise results of previous measurements. The quoted PDG values include SND measurements in  $\eta \rightarrow 3\pi^0$  and  $\eta \rightarrow \pi^+\pi^-\pi^0$  modes [14, 17] based on a part of collected statistics. The present work uses full SND statistics and supersede the results of the measurements [14, 17].

In contrast to previous measurements, the approximation of the  $e^+e^- \rightarrow \eta\gamma$  cross section was performed with free interference phases and therefore the obtained values of the decay probabilities do not depend on model assumptions on these phases. The following values of the phases were obtained:

$$\begin{aligned}\varphi_\omega &= (11.3 \pm 8.1 \pm 0.3)^\circ, \\ \varphi_\phi &= (170 \pm 12 \pm 4)^\circ.\end{aligned}$$

From the ratio of the  $e^+e^- \rightarrow \eta\gamma$  cross sections in two  $\eta$  decay modes, the ratio of the  $\eta$  meson decay probabilities was measured:

$$\frac{\mathcal{B}(\eta \rightarrow 3\pi^0)}{\mathcal{B}(\eta \rightarrow \pi^+\pi^-\pi^0)} = 1.46 \pm 0.03 \pm 0.09.$$

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TABLE III: Cross section ( $\sigma$ ) of the process  $e^+e^- \rightarrow \eta\gamma$  measured in the decay mode  $\eta \rightarrow 3\pi^0$ .  $E$  is center-of-mass energy,  $\delta E$  is its uncertainty,  $IL$  is integrated luminosity,  $N$  is number of selected events with background subtracted,  $\epsilon_0$  is detection efficiency,  $\delta$  is radiative correction. The first error is statistical, the second systematic.

$E$ , MeV	$\delta E$ , MeV	$IL$ , nb $^{-1}$	$N$	$\epsilon_0$	$\delta + 1$	$\sigma$ , nb
599.94	0.16	88.22	$0.0^{+0.5}_{-0.0}$	0.091	0.8424	$< 0.36$ 90%CL
629.96	0.18	117.47	$0.0^{+0.5}_{-0.0}$	0.129	0.8586	$< 0.19$ 90%CL
660.00	0.18	274.29	$2.0^{+1.8}_{-1.0}$	0.142	0.8671	$0.059^{+0.078}_{-0.038}$
689.98	0.20	170.46	$0.0^{+0.5}_{-0.0}$	0.159	0.8712	$< 0.10$ 90%CL
720.00	0.21	575.44	$17.0^{+4.5}_{-3.8}$	0.152	0.8754	$0.22^{+0.07}_{-0.05}$
749.98	0.23	225.20	$10.0^{+3.5}_{-2.8}$	0.152	0.8837	$0.33^{+0.14}_{-0.10}$
760.00	0.24	246.09	$12.0^{+3.8}_{-3.1}$	0.152	0.8848	$0.36^{+0.14}_{-0.10}$
764.00	0.26	258.70	$11.0^{+3.7}_{-3.0}$	0.152	0.8825	$0.32^{+0.13}_{-0.09}$
770.00	0.25	291.87	$21.0^{+4.9}_{-4.3}$	0.152	0.8689	$0.54^{+0.15}_{-0.12}$
773.98	0.25	220.07	$22.0^{+5.0}_{-4.4}$	0.152	0.8452	$0.78^{+0.20}_{-0.17}$
778.00	0.30	259.50	$48.0 \pm 6.9$	0.152	0.8068	$1.50 \pm 0.22$
780.00	0.25	315.38	$60.0 \pm 7.7$	0.152	0.7922	$1.58 \pm 0.21$
780.98	0.24	346.63	$91.0 \pm 9.5$	0.152	0.7913	$2.18 \pm 0.23$
782.00	0.24	664.82	$171.0 \pm 13.1$	0.152	0.7976	$2.13 \pm 0.17$
783.00	0.24	483.13	$119.0 \pm 10.9$	0.152	0.8118	$2.00 \pm 0.19$
783.98	0.24	356.57	$83.0 \pm 9.1$	0.152	0.8324	$1.84 \pm 0.21$
785.02	0.24	221.39	$44.0 \pm 6.6$	0.152	0.8585	$1.52 \pm 0.23$
785.98	0.24	270.02	$48.0 \pm 6.9$	0.152	0.8835	$1.32 \pm 0.19$
789.96	0.25	193.41	$24.0^{+5.2}_{-4.6}$	0.152	0.9651	$0.85^{+0.21}_{-0.17}$
793.96	0.25	211.95	$19.0^{+4.7}_{-4.0}$	0.152	1.004	$0.59^{+0.17}_{-0.13}$
800.00	0.25	284.30	$25.0^{+5.3}_{-4.7}$	0.152	1.021	$0.57^{+0.14}_{-0.11}$
809.98	0.26	286.94	$13.0^{+3.9}_{-3.3}$	0.152	1.021	$0.29^{+0.11}_{-0.08}$
819.94	0.26	321.32	$23.0^{+5.1}_{-4.5}$	0.155	1.010	$0.46^{+0.12}_{-0.09}$
840.00	0.28	692.59	$27.0^{+5.5}_{-4.9}$	0.155	0.9923	$0.25^{+0.06}_{-0.05}$
879.92	0.31	384.26	$11.0^{+3.7}_{-3.0}$	0.155	0.9594	$0.19^{+0.08}_{-0.06}$
919.86	0.35	487.38	$19.0^{+4.7}_{-4.0}$	0.155	0.9312	$0.27^{+0.08}_{-0.06}$
939.88	0.34	488.74	$19.0^{+4.7}_{-4.0}$	0.155	0.9155	$0.27^{+0.08}_{-0.06}$
949.78	0.32	268.39	$6.0^{+2.8}_{-2.1}$	0.155	0.9065	$0.16^{+0.10}_{-0.06}$
957.80	0.32	241.85	$13.0^{+3.9}_{-3.3}$	0.155	0.8981	$0.39^{+0.14}_{-0.11}$
969.80	0.34	258.55	$8.0^{+3.2}_{-2.5}$	0.155	0.8833	$0.23^{+0.11}_{-0.08}$
980.00	0.21	124.62	$4.0^{+2.3}_{-1.7}$	0.152	0.8703	$0.24^{+0.19}_{-0.12}$
984.10	0.37	348.02	$19.0^{+4.7}_{-4.0}$	0.152	0.8624	$0.42^{+0.12}_{-0.09}$
1003.82	0.38	365.59	$72.0 \pm 8.5 \pm 0.3$	0.152	0.8061	$1.60 \pm 0.19$
1009.68	0.39	299.53	$113.0 \pm 10.6 \pm 0.5$	0.152	0.7771	$3.18 \pm 0.31$
1015.64	0.39	344.73	$588.3 \pm 24.3 \pm 2.8$	0.152	0.7324	$15.10 \pm 0.89$
1016.70	0.38	601.93	$1680.7 \pm 41.0 \pm 8.1$	0.152	0.7233	$24.99 \pm 1.26$
1017.66	0.38	937.42	$3659.2 \pm 60.5 \pm 17.6$	0.152	0.7182	$35.44 \pm 1.79$
1018.64	0.39	984.89	$5691.5 \pm 75.4 \pm 27.3$	0.152	0.7238	$53.53 \pm 1.73$
1019.62	0.42	1060.53	$6365.2 \pm 79.8 \pm 30.6$	0.152	0.7544	$54.02 \pm 1.29$
1020.58	0.40	628.02	$3213.9 \pm 56.7 \pm 15.4$	0.152	0.8136	$41.31 \pm 1.70$
1021.64	0.41	325.47	$1056.3 \pm 32.5 \pm 5.1$	0.152	0.9012	$23.32 \pm 1.22$
1022.78	0.39	353.27	$672.4 \pm 25.9 \pm 3.2$	0.152	1.009	$12.24 \pm 0.70$
1027.76	0.40	362.76	$241.2 \pm 15.5 \pm 1.2$	0.152	1.577	$2.76 \pm 0.19$
1033.70	0.39	327.43	$98.8 \pm 9.9 \pm 0.5$	0.152	2.468	$0.80 \pm 0.08$
1039.68	0.39	389.43	$65.0 \pm 8.1 \pm 0.3$	0.152	3.669	$0.30 \pm 0.04$
1049.76	0.39	441.28	$39.3 \pm 6.3 \pm 0.2$	0.152	6.584	$0.089 \pm 0.014$
1059.76	0.44	637.23	$48.3 \pm 7.0 \pm 0.2$	0.152	10.74	$0.046 \pm 0.007$

TABLE IV: Cross section ( $\sigma$ ) of the process  $e^+e^- \rightarrow \eta\gamma$  measured in the decay mode  $\eta \rightarrow 3\pi^0$ .  $E$  is center-of-mass energy,  $\delta E$  is its uncertainty,  $IL$  is integrated luminosity,  $N$  is number of selected events with background subtracted,  $\epsilon_0$  is detection efficiency,  $\delta$  is radiative correction. The first error is statistical, the second systematic.

$E$ , MeV	$\delta E$ , MeV	$IL$ , nb $^{-1}$	$N$	$\epsilon_0$	$\delta + 1$	$\sigma$ , nb
1078.54	3.55	650.05	$18.0^{+4.6}_{-3.9}$	0.0789	24.65	$0.014^{+0.004}_{-0.003}$
1099.92	5.45	605.60	$9.0^{+3.3}_{-2.7}$	0.0769	35.73	$0.005^{+0.002}_{-0.002}$
1131.58	10.49	749.68	$9.0^{+3.3}_{-2.7}$	0.0739	16.39	$0.010^{+0.004}_{-0.003}$
1182.96	15.08	1292.02	$4.0^{+2.3}_{-1.7}$	0.0692	2.816	$0.015^{+0.012}_{-0.007}$
1227.34	11.14	959.07	$1.0^{+1.4}_{-0.5}$	0.0651	1.254	$0.013^{+0.029}_{-0.010}$
1271.68	14.33	1061.97	$3.0^{+2.1}_{-1.4}$	0.0610	0.9952	$0.046^{+0.045}_{-0.025}$
1315.44	11.72	954.60	$1.0^{+1.4}_{-0.5}$	0.0570	0.9465	$0.019^{+0.045}_{-0.016}$
1360.44	14.39	1958.92	$2.0^{+1.8}_{-1.0}$	0.0529	0.9335	$0.021^{+0.027}_{-0.013}$

TABLE V: Cross section ( $\sigma$ ) of the process  $e^+e^- \rightarrow \eta\gamma$  measured in the decay mode  $\eta \rightarrow \pi^+\pi^-\pi^0$ .  $E$  is center-of-mass energy,  $\delta E$  is its uncertainty,  $IL$  is integrated luminosity,  $N$  is number of selected events with background subtracted,  $\epsilon_0$  is detection efficiency,  $\delta$  is radiative correction. The first error is statistical, the second systematic.

$E$ , MeV	$\delta E$ , MeV	$IL$ , nb $^{-1}$	$N$	$\epsilon_0$	$\delta + 1$	$\sigma$ , nb
755.26	5.00	492.5	$5.7 \pm 4.0 \pm 1.0$	0.0695	0.8808	$0.19 \pm 0.13$
769.12	3.98	809.3	$20.7 \pm 8.8 \pm 1.7$	0.0695	0.8683	$0.40 \pm 0.17$
777.96	0.24	264.6	$16.6 \pm 7.7 \pm 0.3$	0.0695	0.8055	$1.12 \pm 0.52$
779.98	0.28	338.5	$22.1 \pm 9.1 \pm 0.4$	0.0640	0.7918	$1.28 \pm 0.53$
780.98	0.24	365.3	$25.6 \pm 9.4 \pm 0.5$	0.0640	0.7909	$1.38 \pm 0.51$
782.00	0.24	697.3	$61.1 \pm 16.4 \pm 1.2$	0.0640	0.7972	$1.71 \pm 0.46$
783.00	0.24	506.3	$59.1 \pm 14.3 \pm 1.2$	0.0640	0.8114	$2.23 \pm 0.54$
783.98	0.24	374.3	$40.0 \pm 11.1 \pm 0.8$	0.0640	0.8319	$1.98 \pm 0.55$
785.02	0.24	232.0	$24.8 \pm 9.0 \pm 0.5$	0.0640	0.8578	$1.92 \pm 0.70$
785.98	0.24	280.7	$22.6 \pm 8.7 \pm 0.5$	0.0640	0.8826	$1.40 \pm 0.54$
792.06	2.02	421.9	$22.7 \pm 7.3 \pm 0.5$	0.0640	0.9875	$0.81 \pm 0.26$
823.36	15.9	1658.6	$33.4 \pm 15.6 \pm 0.7$	0.0640	1.005	$0.30 \pm 0.14$
931.52	28.7	2273.1	$36.7 \pm 14.9 \pm 0.7$	0.0640	0.9319	$0.25 \pm 0.10$
992.14	10.4	907.2	$25.8 \pm 10.9 \pm 0.5$	0.0500	0.8480	$0.54 \pm 0.23$
1009.68	0.39	325.5	$42.0 \pm 13.2 \pm 0.8$	0.0500	0.7778	$3.30 \pm 1.04$
1015.64	0.39	374.7	$209.9 \pm 21.9 \pm 4.2$	0.0500	0.7325	$15.07 \pm 1.74$
1016.70	0.38	660.0	$550.7 \pm 35.9 \pm 11.0$	0.0500	0.7234	$22.70 \pm 1.95$
1017.66	0.38	1028.1	$1383.3 \pm 54.1 \pm 27.7$	0.0500	0.7182	$37.14 \pm 2.42$
1018.64	0.39	1080.9	$1989.2 \pm 65.4 \pm 39.8$	0.0500	0.7238	$51.83 \pm 2.68$
1019.62	0.42	1159.4	$2357.6 \pm 72.6 \pm 47.2$	0.0500	0.7544	$55.63 \pm 2.46$
1020.58	0.40	687.1	$1144.3 \pm 49.3 \pm 22.9$	0.0500	0.8136	$40.87 \pm 2.54$
1021.64	0.41	356.3	$407.3 \pm 29.4 \pm 8.1$	0.0500	0.9012	$24.97 \pm 2.13$
1022.78	0.39	386.9	$237.9 \pm 24.3 \pm 4.8$	0.0500	1.009	$12.01 \pm 1.37$
1027.76	0.40	392.2	$86.9 \pm 14.5 \pm 1.7$	0.0500	1.577	$2.79 \pm 0.47$
1036.96	3.00	777.5	$52.1 \pm 12.2 \pm 1.0$	0.0500	3.078	$0.41 \pm 0.10$
1055.64	4.94	1152.4	$35.7 \pm 15.2 \pm 0.7$	0.0500	9.139	$0.064 \pm 0.027$